

UNIVERSITY OF ILLINOIS  
DIGITAL COMPUTER LABORATORY  
STATISTICAL LIBRARY

KSL 1.20 - 251

TITLE: Centroid Factors with Fixed Communalities (SADOI Only)  
 TYPE: Entire Program  
 CAPACITY: 111 Variables  
 DURATION: TIME IN SECONDS

| Var.<br>n | Input Matrix |          | Per Factor,<br>average | Residual Matrix |          |
|-----------|--------------|----------|------------------------|-----------------|----------|
|           | $d_f=3$      | $d_r=10$ |                        | $d_r=3$         | $d_r=10$ |
| 20        | 7            | 14       | 9                      | 28              | 53       |
| 40        | 27           | 52       | 26                     | 96              | 194      |
| 60        | 60           | 114      | 52                     | 207             | 425      |
| 80        | 107          | 200      | 87                     | 360             | 745      |
| 100       | 166          | 310      | 130                    | 554             | 1154     |
| 111       | 205          | 380      | 157                    | 679             | 1416     |

Add 60 seconds for input of master tape and 15 seconds for parameters and communalities

PARAMETER TAPE: The parameter tape consists of three unsigned decimal numbers separated by fifth-hole characters in the following order:

$f$  space       $f$  - factors to be extracted  
 $d_f$  space       $d_f$  - digits to be punched in factors  
 $d_r$  space       $d_r$  - digits to be punched in residuals

Both  $d_f$  and  $d_r$  may be set to any value less than 12, but the results are accurate to 8 decimal places only. The value of  $f$  must be less than 100. If  $f = 0$ , no factor extraction will take place. If  $d_f = 0$ , and  $f \neq 0$ , the factors will be calculated, but not punched. Only the table of variance removed will be printed. If  $d_r = 0$ , the residual matrix will not be punched.

COMMUNALITIES TAPE: The communalities tape consists of positive signed fractions scaled by  $10^{-1}$ . There must be exactly  $n$  numbers on the tape, and the final number must be terminated by an N.

CORRELATION TAPE: The correlation tape is the lower triangular matrix output of K-8, K-9, or any other triangular matrix of correlations. This tape consists of  $n(n+1)/2$  signed fractions scaled by  $10^{-1}$ . The numbers are punched by rows (i.e.,  $r_{00}$ ,  $r_{10}$ ,  $r_{11}$  ...  $r_{n-1}$ ,  $n-1$ ). The diagonal entries must be present, but it is unimportant what these are, for they are replaced by the communalities.

OPERATOR TAPE: The operator tape is a record of the reflection process. At the beginning of a factor extraction no operator tape is required, for no reflection has taken place. For the extraction of subsequent factors on the same data, see part C under Methods of Use. Part of the output of each

problem consists of this operator tape, so as to permit subsequent continuation of the problem.

METHODS OF USE:

A. To extract f factors and punch out residuals

|                   |              |
|-------------------|--------------|
|                   | <u>Stops</u> |
| 1. Master tape    | 24190        |
| 2. Parameter tape | 2414L        |
| 3. Communalities  | 3418S        |
| 4. Correlations   | 24190        |

At the conclusion of step 4 at stop 24190, another problem can be begun by returning to step 2 and raising the black switch.

B. To extract f factors without residual correlations, set  $d_r = 0$ , and follow steps 1-4 as in A. The final stop will be 240S2. At this point either a new problem can be begun or an additional factor can be extracted.

(1) To begin a new problem raise the black switch. The machine will stop on 24190. Repeat steps 1-4 as in A.

(2) To extract an additional factor, raise the white switch. After the next factor is calculated, the machine will again stop on 240S2. This option may be repeated as many times as desired, each time by raising the white switch.

C. To extract g more factors on a subsequent machine run, first clear the machine as at the beginning of a new problem and read the operator tape. The machine will stop on 2405J. Next read the master tape, and repeat steps as in A, substituting the residual communalities and residual correlations for the original data.

EXAMPLE:

A four-variable example is shown below.

|                         |                       |
|-------------------------|-----------------------|
| 2 space 3 space 3 space | <u>Parameter tape</u> |
| +1+1+1+1N               | <u>Communalities</u>  |
| +100                    | <u>Correlations</u>   |
| +040+100                |                       |
| -055+023+100            |                       |
| -036-030-012+100        |                       |

Results, Factor I

+0.90  
+0.58  
-0.47  
-0.60

N

-0.28  
+0.56  
+0.82  
-0.54

Factor II

N

Table of Per Cent of Variance Removed

|    |         |          |          |
|----|---------|----------|----------|
| NO | ROOT    | PC OF V  | CUM PC   |
| 01 | +01.734 | +043.361 | +043.361 |
| 02 | +01.358 | +033.959 | +077.320 |

EXAMPLE, continued.

RESIDUALS

+0.10  
+0.35  
+0.10  
+0.35N

Residual Communalities

+0.10  
-0.04 +0.35  
-0.10 +0.04 +0.10  
+0.04 -0.35 -0.04 +0.35

Residual Correlations

00689+  
80F00 001F  
00F00 000F  
00F00 002F  
80F00 001F  
24999N

Operator Tape

GENERAL REMARKS:

The purpose of the centroid program is to decompose a matrix of correlations,  $R(n)$ , to a set of  $f$  linearly independent effects or factors. The program calculates the factor matrix,  $F$ , such that

$$R(n) = F F' + R(n-f)$$

where  $R(n-f)$  is the matrix of residual effects. Attempts are often made to reduce the size of the elements of  $R(n-f)$  by introducing communalities estimates which replace the diagonal entries of  $R$ . This program is called the fixed communalities program to distinguish it from other programs which continuously re-estimate the diagonal entries during the course of the calculation.

The  $k$ th factor is obtained merely by dividing the column sums of  $R(n-k)$  by the square root of the total sum of elements of  $R(n-k)$ ; i.e.,

$$f_{ik} = \frac{\sum_j r_{ij}^{(k)}}{\sqrt{\sum_i \sum_j r_{ij}^{(k)}}}$$

The centroid of a set of points is the center of gravity of equal weights at the points. If the axes are so placed that the centroid lies in the first axis of reference, then the centroid has zero projections on all the remaining coordinate axes. It is necessary to rearrange the points to proceed with successive factor extractions. The method chosen here is called the reflection process. To insure that successive effects to be removed from  $R$  are nearly as large as the method permits, whenever the column sum associated with a variable is negative (excluding the diagonal entry), the correlations associated with this variable are changed in sign. The process continues until all of the column sums are either positive or zero. Reflection occurs prior to the extraction of each factor including the first one. It is not necessary for the factor analyst to take this process into account, for a set of operators within the memory keep track of the bookkeeping. The factor loadings which are punched out carry the correct sign which is consistent with the original  $R$ -matrix.

GENERAL REMARKS, continued.

For further discussion of the method, see L.L. Thurstone, Multiple Factor Analysis, University of Chicago Press, 1947, pages 149-75.

NOTE 1:

If the routine stops on an FF order from location 026, raise the white switch. The routine will then print out the per cent of variance removed, the residual communalities, and the residual correlations. A stop on an FF order may be due to any of the following troubles: (1) overfactoring, (2) underestimation of communalities, (3) R-matrix is non-Gramian, (4) machine errors, and (5) errors in data tapes.

NOTE 2:

If the routine stops on an FF order from location 04J, this indicates a failure in transferring orders from the drum to the William's Memory.

|              |                     |
|--------------|---------------------|
| DATE         | January 9, 1959     |
| SUBMITTED BY | <i>K.W. Dickman</i> |
| APPROVED BY  | <i>J. Snyder</i>    |

| LOCATION |      |      | ORDER                 | NOTES                                     | PAGE 1                      |
|----------|------|------|-----------------------|---|-----------------------------|
| Abs.     | Rel. | Sym. |                       |   |                             |
|          |      |      | J                     |   |                             |
|          |      |      | Centroid Factors      |   | Title                       |
|          |      |      | Fixed Communalities   |   |                             |
|          |      |      | 003K                  |   |                             |
| 3        |      | (F)  | 00F 00F               | } by (II)                                 | Factors                     |
| 4        |      | (D)  | 00F 00F               |   | Decimal places in factors   |
| 5        |      | (R)  | 00F 00F               |   | Decimal places in residuals |
| 6        |      | (N)  | 00F 00F               |   | Order of matrix             |
| 7        |      | (T)  | 00F 0064F             |   | No. of words per track      |
| 8        |      | (I)  | 00F 00F               |   | Row number                  |
| 9        |      | (J)  | 00F 00F               | Column number                             |                             |
| 10       |      | (JT) | 00F 00F               | Temporary storage                         |                             |
| 11       |      | (K)  | 00F 00F               | " "                                       |                             |
| 12       |      | (A)  | 00467F 00467F         | Location of drum addresses for vector "j" |                             |
| 13       |      | (V)  | 00578F 00578F         | Location of vector "j"                    |                             |
| 14       |      | (OP) | 00689F 00689F         | Store of operators                        |                             |
| 15       |      | (OI) | 80F 001F              | Control of operators                      |                             |
| 16       |      | (C)  | 00800F 00800F         | Store of communalities                    |                             |
| 17       |      | (S)  | 00911F 00911F         | Store of column sums and factor loadings  |                             |
| 18       |      | (D0) | 8511F 002659F         | Store of r-matrix on drum                 |                             |
| 19       |      | (D1) | 00F 00F               | by 13(II)<br>(D0) - 65                    |                             |
| 20       |      | (D2) | 00F 00F               | by 17(II)<br>(D0) - 4289                  |                             |
| 21       |      | (D3) | 8511F 002560F         | Store of roots on drum                    |                             |
|          |      |      | 00K                   |   |                             |
| 22       |      | (0)  | 00F 00F               | Always zero                               |                             |
| 23       |      | (1)  | 00F 001000 0000 0000J | $10^{-1}$                                 |                             |
| 24       |      | (2)  | 00F 006250 0000 0000J | $2^{-4} \times 10^{+1}$                   |                             |
| 25       |      | (3)  | 00F 003F              | Used to calculate print parameter         |                             |
| 26       |      | (4)  | 00F 0067F             | Used in drum add. routine                 |                             |
| 27       |      | (5)  | 00F 0070F             | Number of digits per line of teletype     |                             |
| 28       |      | (6)  | 40F L521(NL2)         | Test for (NL2)                            |                             |
| 29       |      | (7)  | 26(NL) 00F            | To transfer out of (NL2)                  |                             |
| 30       |      | (8)  | 01F 00F               | To change drum read order to store order  |                             |

| LOCATION |      |      | ORDER          | NOTES       | PAGE 2  | KSL 1.20 |
|----------|------|------|----------------|-------------|---|----------|
| Abs.     | Rel. | Sym. |                |             |   |          |
| 31       |      | (9)  | 00F 00F        | by 26(I1)   | Maximum number of residuals per line                |          |
| 32       |      | (10) | 00F 0010F      |             | Test on input of parameters                         |          |
| 33       |      | (11) | 00F 00F        | by 11(I2)   | Sum of communalities $\times 10^{-2} \times 2^{-2}$ |          |
| 34       |      | (12) | 00F 00F        | by 6(I2)    | (N) - 1   |          |
| 35       |      | (13) | 00F 00F        |             | Temporary storage                                   |          |
| 36       |      | (14) | 00F 00F        |             | " "   |          |
| 37       |      | (15) | 001F 001F      |             | To increase addresses                               |          |
| 38       |      | (16) | FFF 26(M5)     |             | Error stop; white switch to end of program          |          |
| 39       |      | (17) | 00961F 00961F  |             | To adjust (P1)                                      |          |
| 40       |      | (18) | 00642F 00643F  |             | To adjust (P1)                                      |          |
| 41       |      | (19) | 00F 00F        |             | Temporary storage for print of table                |          |
| 42       |      | (20) | 00F 00F        |             | " " " " " "   |          |
| 43       |      | (21) | 00F 00F        |             | " " " " " "   |          |
| 44       |      | (22) | 00F 00F        |             | " " " " " "   |          |
| 45       |      | (Y1) | 00K            |             | To transfer words to and from drum                  |          |
|          |      |      | 00K            |             | To place input routine in memory                    |          |
| 85       | 0    | (M1) | 50335F 50L     |             |   |          |
|          | 1    |      | 26(Y1) 002660F |             |   |          |
|          | 2    |      | 0063F 9259F    |             |   |          |
|          | 3    |      | 50400F 503L    |             |   |          |
|          | 4    |      | 26(Y1) 002726F |             |   |          |
|          | 5    |      | 0062F 24(I1)   |             | Stop for insertion of parameter tape                |          |
|          |      |      | 00K            |             | Read last correlation                               |          |
| 91       | 0    | (M2) | 914F 36L       | from 24(N1) |   |          |
|          | 1    |      | 914F 361L      |             |   |          |
|          |      |      | 00K            |             | To place  |          |
| 93       | 0    |      | 50335F 50L     |             | portions of factor extraction                       |          |
|          | 1    |      | 26(Y1) 002792F |             | routine in memory                                   |          |
|          | 2    |      | 0061F 41(I1)   |             |   |          |
|          | 3    |      | 50400F 503L    |             |   |          |
|          | 4    |      | 26(Y1) 002858F |             |   |          |
|          | 5    |      | 0040F 26(M3)   |             |   |          |
|          |      |      | 00K            |             |   |          |
| 99       | 0    | (M3) | L5(D3) 402(M6) |             | Preset drum add. for store and read                 |          |

| LOCATION |      |      | ORDER           | NOTES                              | PAGE 3                      |
|----------|------|------|-----------------|------------------------------------|-----------------------------|
| Abs.     | Rel. | Sym. |                 |                                    |                             |
|          | 1    |      | L4(8) 406 (M4)  | of roots                           |                             |
|          | 2    |      | L5(18) 466(P1)  | Adjust (P1)                        |                             |
|          | 3    |      | 4222(P1) 41(20) |                                    |                             |
|          | 4    |      | 41(21) 41(22)   |                                    |                             |
|          | 5    |      | L3(F) 36(M9)    | Test: (F) = 0                      |                             |
|          |      |      | 00K             | Main routine                       |                             |
| 105      | 0    | (M4) | 92135F 50L      |                                    |                             |
|          | 1    |      | 26(SJ) 501L     | Column sums                        |                             |
|          | 2    |      | 26(RF) 41F      | Reflection process                 |                             |
|          | 3    |      | 9259F 503L      |                                    |                             |
|          | 4    |      | 26(CL) 504L     | Calculate factor loadings          |                             |
|          | 5    |      | 26(PL) 15(14)   | Print factor loadings              |                             |
|          | 6    |      | 00F 00F         | Drum address                       |                             |
|          | 7    |      | F56L 406L       | for store of root                  |                             |
|          | 8    |      | 50(0) 508L      |                                    |                             |
|          | 9    |      | 26(RC) 509L     |                                    |                             |
|          | 10   |      | 26(RR) F5(19)   | Residual communalities             |                             |
|          | 11   |      | 42(19) 10(F)    | Residual correlations              |                             |
|          | 12   |      | 36(M5) 26L      | Test for end of factor extraction. |                             |
|          |      |      | 00K             |                                    |                             |
| 118      | 0    | (M5) | 92135F 92259F   | from 12 (M4)                       | Title for table of variance |
|          | 1    |      | 92965F 92770F   |                                    |                             |
|          | 2    |      | 92578F 92965F   |                                    |                             |
|          | 3    |      | 92258F 92582F   |                                    |                             |
|          | 4    |      | 92322F 92977F   |                                    |                             |
|          | 5    |      | 922F 92835F     |                                    |                             |
|          | 6    |      | 92961F 92578F   |                                    |                             |
|          | 7    |      | 92898F 92961F   |                                    |                             |
|          | 8    |      | 92323F 92977F   |                                    |                             |
|          | 9    |      | 92835F 92450F   |                                    |                             |
|          | 10   |      | 92643F 92961F   |                                    |                             |
|          | 11   |      | 922F 92835F     |                                    |                             |
|          | 12   |      | 92707F 92519F   |                                    |                             |

| LOCATION |              |       | ORDER            | NOTES       | PAGE 4                          |
|----------|--------------|-------|------------------|-------------|---------------------------------|
| Abs.     | Rel.         | Sym.  |                  |             |                                 |
| 131      | 0            | (M6)  | 00K              |             | Take roots off drum             |
|          | 1            |       | L5(S) 423L       |             |                                 |
|          | 2            |       | 421(M7) 92135F   |             |                                 |
|          | 3            |       | 00F 00F          | by 0(M3)    | Drum address                    |
|          | 4            |       | 223L 40F         | by 0(M6)    |                                 |
|          | 5            |       | F52L 402L        |             |                                 |
|          | 6            |       | F53L 423L        |             |                                 |
|          | 7            |       | F5(22) 42(22)    |             |                                 |
| 140      | 8            | (M7)  | 10(F) 36(M7)     |             |                                 |
|          | 8            |       | 262L 00F         |             |                                 |
|          | 0            |       | 00K              |             | Print table of variance         |
|          | 1            |       | L5(17) 466(P1)   |             |                                 |
|          | 2            |       | 4222(P1) L5F     |             |                                 |
|          | 3            |       | 40(K) F5(21)     |             |                                 |
|          | 4            |       | J022F 503L       |             |                                 |
|          | 5            |       | 26(P1) L5(18)    |             | Factor number                   |
|          | 6            |       | 466(P1) 4222(P1) |             |                                 |
|          | 7            |       | L5(K) 002F       |             |                                 |
|          | 8            |       | 5252F 507L       |             |                                 |
|          | 9            |       | 26(P1) 92961F    |             | Root                            |
|          | 10           |       | L5(K) 66(11)     |             |                                 |
|          | 11           |       | 75(1) 40(JT)     |             |                                 |
|          | 12           |       | 5263F 5011L      |             |                                 |
|          | 13           |       | 26(P1) 92965F    |             | Per cent of variance            |
|          | 14           |       | L5(JT) L4(20)    |             |                                 |
|          | 15           |       | 40(20) 50(1)     |             |                                 |
|          | 16           |       | 5263F 5015L      |             | Cumulative per cent of variance |
|          | 17           |       | 26(P1) 92131F    |             |                                 |
| 18       | 92515F F51L  |       |                  |             |                                 |
| 19       | 421L F5(21)  |       |                  |             |                                 |
| 20       | 42(21) 10(F) |       |                  |             |                                 |
| 161      |              | (M71) | 36(M71) 26L      |             |                                 |
|          |              |       | 00K              |             |                                 |
|          |              |       | 92135F 92259F    | from 20(M7) |                                 |



| LOCATION |      |             | ORDER               | NOTES  | PAGE 5  |
|----------|------|-------------|---------------------|--|---|
| Abs.     | Rel. | Sym.        |                     |  |   |
| 162      | 0    | (M8)        | 00K<br>9259F 92135F |  | Print residual<br>communalities $\times 10^{-1}$  |
|          | 1    |             | L3(D) 36(M9)        |  |   |
|          | 2    |             | L5(C) 424L          |  |   |
|          | 3    |             | L5(D) 466L          |  |   |
|          | 4    |             | 41(I) 50F           | by 2L  |   |
|          | 5    |             | 75(2) 004F          |  |   |
|          | 6    |             | 52F 506L            |  |   |
|          | 7    |             | 26(P1) F54L         |  |   |
|          | 8    |             | 424L F5(I)          |  |   |
|          | 9    |             | 42(I) L0(N)         |  |   |
|          | 10   |             | 3211L 92131F        |  |   |
| 11       |      | 224L 92770F |                     |  |   |
| 174      | 0    | (M9)        | 00K<br>L3(R) 367L   | from 1(M9)   | To place routine to<br>print residuals in<br>memory<br>To test: (R) = 0   |
|          | 1    |             | 50335F 501L         |  |   |
|          | 2    |             | 26(Y1) 002990F      |  |   |
|          | 3    |             | 0040F 92139F        |  |   |
|          | 4    |             | 50400F 504L         |  |   |
|          | 5    |             | 26(Y1) 003056F      |  |   |
|          | 6    |             | 0030F 26(PR)        |  |   |
|          | 7    |             | F5(F) 42(F)         |  |   |
| 8        |      | 241L 26(M4) |                     | If (R) = 0, option: black switch yields<br>new problem, white switch calculates<br>another factor. |   |
| 183      |      | (P1)        | 00K<br>Insert (P1)  |  | Print routine   |
| 211      | 0    | (V1)        | 00K<br>K5F 4230L    | from 6(SJ)<br>or 21(RF)  | Routine to pre-calculate<br>addresses of vector "j"<br>and read a column from a<br>triangular matrix stored on drum |
|          | 1    |             | L5(A) 4212L         |  |   |
|          | 2    |             | 4223L L4(12)        |  |   |
|          | 3    |             | 4231L L5(V)         |  |   |
|          | 4    |             | 4226L 41(I)         |  |   |
|          | 5    |             | 50(J) 75(T)         |  |   |
| 6        |      | S5F 40(JT)  |                     |  |   |

| LOCATION |      |      | ORDER        | NOTES       | PAGE 6                      |
|----------|------|------|--------------|-------------|-----------------------------|
| Abs.     | Rel. | Sym. |              |             |                             |
|          | 7    |      | L5(I) L0(J)  |             |                             |
|          | 8    |      | 40(K) 3619L  |             |                             |
|          | 9    |      | L5(J) L0(4)  |             |                             |
|          | 10   |      | 3216L L5(JT) |             |                             |
|          | 11   |      | L4(D1) L4(J) |             |                             |
|          | 12   |      | L4(I) 40F    | by 1(V1)    | Drum order for element i, j |
|          | 13   |      | F512L 4212L  |             |                             |
|          | 14   |      | F5(I) 42(I)  |             |                             |
|          | 15   |      | L0(N) 3223L  |             |                             |
|          | 16   |      | 267L 50(0)   |             |                             |
|          | 17   |      | L5(JT) 001F  |             |                             |
|          | 18   |      | L4(D2) 2211L |             |                             |
|          | 19   |      | L1(K) 3614L  |             |                             |
|          | 20   |      | 50(I) 75(T)  |             |                             |
|          | 21   |      | S5F 40(JT)   |             |                             |
|          | 22   |      | L5(I) 229L   |             |                             |
|          | 23   |      | 00F L5F      |             |                             |
|          | 24   |      | 4025L 3225L  |             |                             |
|          | 25   |      | 00F 00F      | by 24L      | Drum address                |
|          | 26   |      | 3226L 40F    | by 4L       | Store                       |
|          | 27   |      | F526L 4226L  |             |                             |
|          | 28   |      | F523L 4223L  |             |                             |
|          | 29   |      | L031L 3223L  |             |                             |
|          | 30   |      | 001F 22F     |             |                             |
|          | 31   |      | 80F L5F      |             |                             |
|          |      |      | 00K          |             | Reflect vector "j"          |
| 243      | 0    | (RN) | K5F 4216L    | from 22(RF) | and replace on drum         |
|          | 1    |      | L5(A) 426L   |             |                             |
|          | 2    |      | 427L 4210L   |             |                             |
|          | 3    |      | L4(12) 4218L |             |                             |
|          | 4    |      | L5(V) 4211L  |             |                             |
|          | 5    |      | L4(12) 4217L |             |                             |
|          | 6    |      | 50(0) L5F    | by 11(RN)   |                             |
|          | 7    |      | L4(8) 40F    | by 2(RN)    |                             |
|          | 8    |      | F56L 426L    |             |                             |

| LOCATION |      |      | ORDER         | NOTES      | PAGE 7   |
|----------|------|------|---------------|------------|--|
| Abs.     | Rel. | Sym. |               |            |  |
|          | 9    |      | 427L L018L    |            |  |
|          | 10   |      | 326L L5F      |            |  |
|          | 11   |      | 4012L L1F     |            |  |
|          | 12   |      | 00F 00F       | by 11(RN)  | Drum address precalculated                             |
|          | 13   |      | F510L 4210L   |            |  |
|          | 14   |      | F511L 4211L   |            |  |
|          | 15   |      | L017L 3210L   |            |  |
|          | 16   |      | 00LF 22F      |            |  |
|          | 17   |      | N012L L1F     |            |  |
|          | 18   |      | J0(0) L5F     |            |  |
|          |      |      | 00K           |            | Calculate column sums                                  |
| 262      | 0    | (SJ) | K5F 4215L     | From 1(M4) |  |
|          | 1    |      | L5(S) 4212L   |            |  |
|          | 2    |      | 41(J) 41(13)  |            |  |
|          | 3    |      | F5(13) 42(13) |            |  |
|          | 4    |      | L5(V) 426L    |            |  |
|          | 5    |      | 41(14) 505L   |            |  |
|          | 6    |      | 26(V1) L5F    | by 4(M4)   |  |
|          | 7    |      | L4(14) 40(14) |            |  |
|          | 8    |      | F56L 426L     |            |  |
|          | 9    |      | F5(13) 42(13) |            |  |
|          | 10   |      | L0(N) 3612L   |            |  |
|          | 11   |      | 226L 00F      |            |  |
|          | 12   |      | L5(14) 40F    | by 1(SJ)   | Column sums at (S)                                     |
|          | 13   |      | F512L 4212L   |            |  |
|          | 14   |      | F5(J) 42(J)   |            |  |
|          | 15   |      | L0(N) 32F     |            |  |
|          | 16   |      | 222L 00F      |            |  |
|          |      |      | 00K           |            | Reflection process                                     |
| 279      | 0    | (RF) | K5F 4218L     | from 2(M4) | continue to reflect until all column sums are positive |
|          | 1    |      | 41(I) L5(S)   |            |  |
|          | 2    |      | 40F 402F      |            |  |
|          | 3    |      | 425L 465L     |            |  |
|          | 4    |      | 4229L 4629L   |            |  |
|          | 5    |      | L1F L4F       | by 3(RF)   | Select lowest column                                   |

| LOCATION |      |      | ORDER         | NOTES      | PAGE 8                 |
|----------|------|------|---------------|------------|------------------------|
| Abs.     | Rel. | Sym. |               |            |                        |
|          | 6    |      | 369L L52F     |            | sum, $S_j$             |
|          | 7    |      | 40F 0020F     |            |                        |
|          | 8    |      | 465L 265L     |            |                        |
|          | 9    |      | F52F 422F     |            |                        |
|          | 10   |      | 425L F5(I)    |            |                        |
|          | 11   |      | 42(I) L0(N)   |            |                        |
|          | 12   |      | 3613L 265L    |            |                        |
|          | 13   |      | L5F 4217L     |            |                        |
|          | 14   |      | 40(13) L0(S)  |            |                        |
|          | 15   |      | 42(J) L4(OP)  |            | Test: $S_j < 0$        |
|          | 16   |      | 4219L 0020F   |            |                        |
|          | 17   |      | 4620L FLF     |            |                        |
|          | 18   |      | 3619L 22F     |            |                        |
|          | 19   |      | L5(01) L4F    | by 16(RF)  | Adjust operator        |
|          | 20   |      | 40F 5020L     | by 17(RF)  |                        |
|          | 21   |      | 26(V1) 5021L  |            |                        |
|          | 22   |      | 26(RN) L5(13) |            | Reflect vector         |
|          | 23   |      | 4224L 0020F   |            |                        |
|          | 24   |      | 4625L L1F     | by 23(RF)  |                        |
|          | 25   |      | 40F L5(V)     | by 24(RF)  |                        |
|          | 26   |      | 4628L 41(14)  |            |                        |
|          | 27   |      | L3(J) 3231L   |            |                        |
|          | 28   |      | L1F 001F      | by 26(RF)  | Adjust column sums on  |
|          | 29   |      | L4F 40F       | by 4(RF)   | Williams memory        |
|          | 30   |      | L528L L4(15)  |            |                        |
|          | 31   |      | 4628L L529L   |            |                        |
|          | 32   |      | L4(15) 4029L  |            |                        |
|          | 33   |      | F5(14) 42(14) |            |                        |
|          | 34   |      | L0(J) 401F    |            |                        |
|          | 35   |      | L31F 3231L    |            |                        |
|          | 36   |      | L5(14) L0(N)  |            |                        |
|          | 37   |      | 361L 2628L    |            |                        |
|          |      |      | 00K           |            | Residual communalities |
| 317      | 0    | (RC) | K5F 4212L     | from 9(M4) |                        |
|          | 1    |      | L5(C) 426L    |            |                        |

| LOCATION |      |       | ORDER           | NOTES       | PAGE 9                                     |
|----------|------|-------|-----------------|-------------|--|
| Abs.     | Rel. | Sym.  |                 |             |  |
|          | 2    |       | 427L L5(S)      |             |  |
|          | 3    |       | 425L 465L       |             |  |
|          | 4    |       | 41(K) 50(O)     |             |  |
|          | 5    |       | 50F 7JF         | by 3(RC)    |  |
|          | 6    |       | 401F L5F        | by 1(RC)    | $r_{ii}^{(k)} = r_{ii}^{(k-1)} - f_{ik}^2$ |
|          | 7    |       | L01F 40F        | by 2(RC)    |  |
|          | 8    |       | L55L L4(15)     |             |  |
|          | 9    |       | 405L F56L       |             |  |
|          | 10   |       | 426L 427L       |             |  |
|          | 11   |       | F5(K) 42(K)     |             |  |
|          | 12   |       | L0(N) 32F       |             |  |
|          | 13   |       | 265L 00F        |             |  |
|          |      |       | 00335K (PR)(I2) |             |  |
| 335      |      | (RL)  | 00335K          |             | Square root routine                        |
|          |      |       | 00K             |             | Calculate factor                           |
| 344      | 0    | (CL)  | K5F 4222L       | from 4(M4)  | loadings                                   |
|          | 1    |       | L5(C) 466L      |             |  |
|          | 2    |       | L5(S) 426L      |             |  |
|          | 3    |       | 427L 4617L      |             |  |
|          | 4    |       | 4218L 41(14)    |             |  |
|          | 5    |       | 41(K) 41(J)     |             |  |
|          | 6    |       | L5F L4F         | by 1 and 2L | $(C_j + S_j) \times 10^{-2} \times 2^{-4}$ |
|          | 7    | (I3)  | 104F 40F        | by 3L       |  |
|          | 8    |       | 104F L4(14)     |             |  |
|          | 9    |       | 40(14) L56L     |             | Sum of $(C_j + S_j) \times 10^{-2}$        |
|          | 10   |       | L4(15) 406L     |             | $\times 2^{-8}$ at (14)                    |
|          | 11   |       | 427L F5(K)      |             |  |
|          | 12   | (NL2) | 42(K) L0(N)     |             |  |
|          | 13   |       | 3614L 266L      |             |  |
|          | 14   |       | L5(14) 3215L    |             |  |
|          | 15   |       | 26(16) 5015L    |             | Test: (14) < 0; if positive                |
|          | 16   |       | 26(RL) 40(14)   |             | take square root of (14)                   |
|          | 17   |       | L5F 66(14)      |             |  |
|          | 18   |       | S5F 40F         | by 4(CL)    | $ f_{ik}  \times 10^{-1}$                  |
|          | 19   |       | F518L 4218L     |             |  |

| LOCATION |      |      | ORDER                 | NOTES       | PAGE 10 | KSL 1.20                                      |
|----------|------|------|-----------------------|-------------|---------|---|
| Abs.     | Rel. | Sym. |                       |             |         |   |
|          | 20   |      | 0020F 4617L           |             |         |   |
|          | 21   |      | F5(J) 42(J)           |             |         |   |
|          | 22   |      | L0(N) 32F             |             |         |   |
|          | 23   |      | 2617L 00F             |             |         |   |
|          |      |      | 00K                   |             |         | Print factor loadings                         |
| 368      | 0    | (PL) | <del>K5</del> F 4225L | from 5(M4)  |         |   |
|          | 1    |      | L5(OP) 426L           |             |         |   |
|          | 2    |      | L5(S) 427L            |             |         |   |
|          | 3    |      | 4215L 41(14)          |             |         |   |
|          | 4    |      | L3(D) 3617L           |             |         | Test: (D) = 0                                 |
|          | 5    |      | L5(D) 468L            |             |         |   |
|          | 6    |      | 41(K) L5F             | by 1(PL)    |         | Test operator: print + $f_{ik}$ or - $f_{ik}$ |
|          | 7    |      | 3215L L1F             |             |         |   |
|          | 8    |      | 52F 508L              |             |         |   |
|          | 9    |      | 26(PL) 92131F         |             |         |   |
|          | 10   |      | F56L 426L             |             |         |   |
|          | 11   |      | F57L 427L             |             |         |   |
|          | 12   |      | 4215L F5(K)           |             |         |   |
|          | 13   |      | 42(K) L0(N)           |             |         |   |
|          | 14   |      | 3216L 226L            |             |         |   |
|          | 15   |      | 00F L5F               | from 7(PL)  |         |   |
|          | 16   |      | 228L 92770F           |             |         |   |
|          | 17   |      | 41(K) L5(S)           |             |         |   |
|          | 18   |      | 4220L 4620L           |             |         |   |
|          | 19   |      | 2120L S5F             |             |         |   |
|          | 20   |      | 50F 74F               | by 18(PL)   |         |   |
|          | 21   |      | 102F L4(14)           |             |         | Sum of squares of                             |
|          | 22   |      | 40(14) L520L          |             |         | factor loadings                               |
|          | 23   |      | L4(15) 4020L          |             |         |   |
|          | 24   |      | F5(K) 42(K)           |             |         |   |
|          | 25   |      | L0(N) 32F             |             |         |   |
|          | 26   |      | 2219L 00F             |             |         |   |
|          |      |      | 00400K (PO)(I1)       |             |         | To calculate residual                         |
| 400      | 0    | (RR) | <del>K5</del> F 423L  | from 10(M4) |         | correlations                                  |
|          | 1    |      | 41(J) 41(I)           |             |         |   |

| LOCATION |      |      | ORDER        | NOTES     | PAGE 11                         |
|----------|------|------|--------------|-----------|---------------------------------|
| Abs.     | Rel. | Sym. |              |           |                                 |
|          | 2    |      | F5(J) 42(J)  |           |                                 |
|          | 3    |      | L0(N) 32F    |           |                                 |
|          | 4    |      | L5(S) 4225L  |           | Take triangular matrix          |
|          | 5    |      | L4(J) 0020F  |           | off drum, a row at a            |
|          | 6    |      | 4625L L5(V)  |           | time, and calculate             |
|          | 7    |      | 4216L 4226L  |           | $r_{ij}^{(k)} = r_{ij}^{(k-1)}$ |
|          | 8    |      | 4232L 4626L  |           |                                 |
|          | 9    |      | 41(I) L5(J)  |           | $- f_{ik} f_{jk}$               |
|          | 10   |      | L0(4) 3221L  |           |                                 |
|          | 11   |      | 50(J) 75(T)  |           | then replace on drum            |
|          | 12   |      | L5(D1) L4(J) |           |                                 |
|          | 13   |      | S4F 4015L    |           |                                 |
|          | 14   |      | L4(8) 4033L  |           |                                 |
|          | 15   |      | 00F 00F      | by 13(RR) | drum address                    |
|          | 16   |      | 3216L 40F    | by 7(RR)  |                                 |
|          | 17   |      | F515L 4015L  |           |                                 |
|          | 18   |      | F516L 4216L  |           |                                 |
|          | 19   |      | F5(I) 42(I)  |           |                                 |
|          | 20   |      | L0(J) 3224L  |           |                                 |
|          | 21   |      | 2615L 50(J)  |           |                                 |
|          | 22   |      | 75(T) 001F   |           |                                 |
|          | 23   |      | L5(D2) 2212L |           |                                 |
|          | 24   |      | 00F 41(I)    |           |                                 |
|          | 25   |      | 50F 71F      | by 6(RR)  |                                 |
|          | 26   |      | L4F 40F      | by 7(RR)  |                                 |
|          | 27   |      | F525L 4225L  |           |                                 |
|          | 28   |      | L526L L4(15) |           |                                 |
|          | 29   |      | 4026L F5(I)  |           |                                 |
|          | 30   | (N1) | 42(I) L0(J)  |           |                                 |
|          | 31   |      | 3632L 2625L  |           |                                 |
|          | 32   |      | 41(I) L5F    | by 8(RR)  |                                 |
|          | 33   |      | 00F 00F      | by 14(RR) | drum address                    |
|          | 34   |      | F532L 4232L  |           |                                 |
|          | 35   |      | F533L 4033L  |           |                                 |
|          | 36   |      | F5(I) 42(I)  |           |                                 |

| LOCATION |      |      | ORDER                  | NOTES       | PAGE 12                                   |
|----------|------|------|------------------------|-------------|---|
| Abs.     | Rel. | Sym. |                        |             |   |
|          | 37   |      | L0(J) 362L             |             |   |
|          | 38   |      | 2232L 00F              |             |   |
|          |      |      | 00911K                 |             | Store Drum Set I                          |
| 911      | 0    |      | J0335F 50L             |             |   |
|          | 1    |      | 26(YL) 002792F         |             |   |
|          | 2    |      | 0061F 263L             |             |   |
|          | 3    |      | J0400F 503L            |             |   |
|          | 4    |      | 26(YL) 002858F         |             |   |
|          | 5    |      | 0040F 26999F<br>26911N |             |   |
|          |      |      | 00335K                 |             | Input communalities tape                  |
| 355      | 0    | (I2) | I5(C) 46(6)            | from 29(I1) |   |
|          | 1    |      | 463L 428L              |             |   |
|          | 2    |      | 429L 41(J)             |             |   |
|          | 3    |      | 50F 503L               |             |   |
|          | 4    |      | 26(NL2) L521(NL2)      |             |   |
|          | 5    |      | L0(6) 1020F            |             |   |
|          | 6    |      | 40(N) F0(0)            |             | Store order of matrix at (N)              |
|          | 7    |      | 40(I2) 41(I)           |             |   |
|          | 8    |      | 41(I1) 50F             |             |   |
|          | 9    |      | 75(1) 40F              |             | $C_j \times 10^{-2}$                      |
|          | 10   |      | 102F L4(I1)            |             |   |
|          | 11   |      | 40(I1) F58L            |             | Sum of $C_j \times 10^{-2} \times 2^{-2}$ |
|          | 12   |      | 428L 429L              |             | at (I1)                                   |
|          | 13   |      | F5(J) 42(J)            |             |   |
|          | 14   |      | L0(N) 34(I6)           |             | Stop for insertion of R-tape              |
|          | 15   |      | 228L 00F               |             |   |
|          |      |      | 00K                    |             | Input correlations tape                   |
| 351      | 0    | (I3) | L5(S) 463L             | from (I6)   |   |
|          | 1    |      | L4(I5) 46(6)           |             |   |
|          | 2    |      | L5(7) 4022(NL2)        |             |   |
|          | 3    |      | 50F 503L               |             |   |
|          | 4    |      | 26(NL2) 222(NL)        |             |   |



| LOCATION |      |       | ORDER        | NOTES       | PAGE 13                          |
|----------|------|-------|--------------|-------------|----------------------------------|
| Abs.     | Rel. | Sym.  |              |             |                                  |
| 356      |      | (NL2) | 00K          |             | Input routine (NL2)              |
|          |      |       | 00K          |             |                                  |
| 395      |      | (I6)  | 41(J) 26(I3) | from 14(I2) |                                  |
|          |      |       | 00400K       |             |                                  |
| 400      | 0    | (I1)  | 192F 401F    | from 5(M1)  | Input parameters & f space       |
|          | 1    |       | L5(3) 428L   |             | d <sub>r</sub> space             |
|          | 2    |       | 41F 914F     |             | d <sub>r</sub> space             |
|          | 3    |       | 325L 222L    |             |                                  |
|          | 4    |       | 914F 325L    |             |                                  |
|          | 5    |       | 268L 50F     |             |                                  |
|          | 6    |       | 74(10) S5F   |             |                                  |
|          | 7    |       | 40F 264L     |             |                                  |
|          | 8    |       | L5F 40F      | by 1(I1)    |                                  |
|          | 9    |       | F58L 428L    |             |                                  |
|          | 10   |       | L51F L41F    |             |                                  |
|          | 11   |       | 401F 362L    |             |                                  |
|          | 12   |       | L5(D0) F0(T) |             |                                  |
|          | 13   |       | 40(D1) F5(T) |             | Form (D1) and (D2)               |
|          | 14   |       | 40F 50F      |             |                                  |
|          | 15   |       | 75F L5(D0)   |             |                                  |
|          | 16   |       | L0(T) S0F    |             |                                  |
|          | 17   |       | 40(D2) L3(D) |             | Calculate print parameter        |
|          | 18   |       | 3621L 50(D)  |             |                                  |
|          | 19   |       | 75(10) K5F   |             |                                  |
|          | 20   |       | 0020F 46(D)  |             |                                  |
|          | 21   |       | L3(R) 3629L  |             |                                  |
|          | 22   |       | L5(R) L4(3)  |             |                                  |
|          | 23   |       | 008F 40F     |             |                                  |
|          | 24   |       | L5(5) 66F    |             |                                  |
|          | 25   |       | S5F 1031F    |             |                                  |
|          | 26   |       | 40(9) 50(R)  |             | Store number of residuals        |
|          | 27   |       | 75(10) K5F   |             | per line at (9)                  |
|          | 28   |       | 0020F 46(R)  |             |                                  |
|          | 29   |       | 24(I2) 00F   |             | Transfer to C <sub>j</sub> input |

| LOCATION |      |      | ORDER                       | NOTES | PAGE 14   |
|----------|------|------|-----------------------------|-------|---|
| Abs.     | Rel. | Sym. |                             |       |   |
|          |      |      | 00K                         |       |   |
| 430      | 0    | (N1) | L4(N12) 4621(N12) from(N12) |       | Addition to (N12) to read in a triangular matrix, to calculate drum addresses, and store on drum.<br><br>$r_{ij} \times 10^{-2}$<br><br>Drum order<br><br>Store Drum Set II |
|          | 1    |      | L5(6) L021(N12)             |       |   |
|          | 2    |      | 3623(N12) L5(6)             |       |   |
|          | 3    |      | L4(N12) 46(6)               |       |   |
|          | 4    |      | 1020F 4228L                 |       |   |
|          | 5    |      | 4229L F5(S)                 |       |   |
|          | 6    |      | 428L 429L                   |       |   |
|          | 7    |      | 4218L 4621(N12)             |       |   |
|          | 8    |      | 41(I) 50F                   |       |   |
|          | 9    |      | 75(1) 40F by 6(N1)          |       |   |
|          | 10   |      | F58L 428L                   |       |   |
|          | 11   |      | 429L L028L                  |       |   |
|          | 12   |      | 328L F5(J)                  |       |   |
|          | 13   |      | 42(J) L0(4)                 |       |   |
|          | 14   |      | 3625L 50(0)                 |       |   |
|          | 15   |      | 50(J) 75(T)                 |       |   |
|          | 16   |      | L5(D1) S4F                  |       |   |
|          | 17   |      | L4(J) L4(8)                 |       |   |
|          | 18   |      | 4019L L5F                   |       |   |
|          | 19   |      | 00F 00F by 18L              |       |   |
|          | 20   |      | F519L 4019L                 |       |   |
|          | 21   |      | F518L 4218L                 |       |   |
|          | 22   |      | L029L 3218L                 |       |   |
|          | 23   |      | L5(J) L0(L2)                |       |   |
|          | 24   |      | 36(M2) 2623(N12)            |       |   |
|          | 25   |      | 50(J) 75(T)                 |       |   |
|          | 26   |      | 001F L5(D2)                 |       |   |
|          | 27   |      | 2216L 00F                   |       |   |
|          | 28   |      | N1(I) 50F                   |       |   |
|          | 29   |      | N019L L5F                   |       |   |
|          |      |      | 00911K                      |       |   |
| 411      | 0    |      | J0335F 50L                  |       |   |
|          | 1    |      | 26(Y1) 002660F              |       |   |
|          | 2    |      | 0063F 263L                  |       |   |

| Abs. | Rel. | Sym. |                |        |                |
|------|------|------|----------------|--------|----------------|
|      | 3    |      | J0400F 503L    |        |                |
|      | 4    |      | 26(Y1) 002726F |        |                |
|      | 5    |      | 0062F 26999F   |        |                |
|      |      |      | 26911N         |        |                |
|      |      |      | 00335K         |        |                |
| 335  |      | (PR) | L3(R) 3621(PO) |        | Test: (R) = 0  |
|      |      |      | 00K            |        | Print residual |
| 336  | 0    |      | L5(R) 466L     |        | correlations   |
|      | 1    |      | 4630L 9259F    |        |                |
|      | 2    |      | 92135F L5(C)   |        |                |
|      | 3    |      | 424L 41(J)     |        |                |
|      | 4    |      | 41(I) 50F      | by 3L  |                |
|      | 5    |      | 75(2) 004F     |        |                |
|      | 6    |      | 52F 506L       |        |                |
|      | 7    |      | 26(P1) 92135F  |        |                |
|      | 8    |      | 92519F F54L    |        |                |
|      | 9    |      | 424L F5(J)     |        |                |
|      | 10   |      | 42(J) L0(N)    |        |                |
|      | 11   |      | 36(PO) 41(I)   |        |                |
|      | 12   |      | L5(V) 4219L    |        |                |
|      | 13   |      | 4228L L5(J)    |        |                |
|      | 14   |      | L0(4) 3224L    |        |                |
|      | 15   |      | 50(J) 75(T)    |        |                |
|      | 16   |      | L5(D1) L4(J)   |        |                |
|      | 17   |      | S4F 4018L      |        |                |
|      | 18   |      | Q0F 00F        | by 17L | Drum address   |
|      | 19   |      | 3219L 40F      | by 12L |                |
|      | 20   |      | F518L 4018L    |        |                |
|      | 21   |      | F519L 4219L    |        |                |
|      | 22   |      | F5(I) 42(I)    |        |                |
|      | 23   |      | L0(J) 3227L    |        |                |
|      | 24   |      | 2618L 50(J)    |        |                |
|      | 25   |      | 75(T) 001F     |        |                |
|      | 26   |      | L5(D2) 2216L   |        |                |
|      | 27   |      | 00F 41(I)      |        |                |
|      | 28   |      | 41(K) 50F      | by 13L |                |

| LOCATION |      |      | ORDER                  | NOTES     | PAGE 16             | KSL 1.20 |
|----------|------|------|------------------------|-----------|---------------------|----------|
| Abs.     | Rel. | Sym. |                        |           |                     |          |
|          | 29   |      | 75(2) 004F             |           |                     |          |
|          | 30   |      | 52F 5030L              |           |                     |          |
|          | 31   |      | 26(P1) F5(K)           |           |                     |          |
|          | 32   |      | 42(K) L0(9)            |           |                     |          |
|          | 33   |      | 3634L 2235L            |           |                     |          |
|          | 34   |      | 92131F 92519F          |           |                     |          |
|          | 35   |      | 41(K) F528L            |           |                     |          |
|          | 36   |      | 4228L F5(I)            |           |                     |          |
|          | 37   |      | 42(I) L0(J)            |           |                     |          |
|          | 38   |      | 324L 2228L             |           |                     |          |
|          |      |      | 00400K                 |           |                     |          |
| 400      | 0    | (PO) | 92981F 9259F           | from 347F | Print operator tape |          |
|          | 1    |      | 92135F 41(I)           |           |                     |          |
|          | 2    |      | 922F 922F              |           |                     |          |
|          | 3    |      | L5(17) 466(P1)         |           |                     |          |
|          | 4    |      | L5(18) L0(15)          |           |                     |          |
|          | 5    |      | 4222(P1) <b>L5(OP)</b> |           |                     |          |
|          | 6    |      | 1020F 4210L            |           |                     |          |
|          | 7    |      | J033F 507L             |           |                     |          |
|          | 8    |      | 26(P1) 92131F          |           |                     |          |
|          | 9    |      | L512L 1020F            |           |                     |          |
|          | 10   |      | 4222(P1) L5F           |           |                     |          |
|          | 11   |      | 42(J) 828F             |           |                     |          |
|          | 12   |      | 92898F L5(J)           |           |                     |          |
|          | 13   |      | J055F 5013L            |           |                     |          |
|          | 14   |      | 26(P1) 92131F          |           |                     |          |
|          | 15   |      | F510L 4210L            |           |                     |          |
|          | 16   |      | F5(I) 42(I)            |           |                     |          |
|          | 17   |      | L0(N) 3218L            |           |                     |          |
|          | 18   |      | 2210L 92130F           |           |                     |          |
|          | 19   |      | 92258F 92586F          |           |                     |          |
|          | 20   |      | 92770F 92981F          |           |                     |          |
|          | 21   |      | 921001F L5(OP)         |           |                     |          |
|          | 22   |      | 4223L L4(N)            |           |                     |          |

| LOCATION |      |      | ORDER          | NOTES | PAGE 17            |
|----------|------|------|----------------|-------|--------------------|
| Abs.     | Rel. | Syn. |                |       |                    |
|          | 23   |      | 4227L 41F      |       |                    |
|          | 24   |      | F523L 4223L    |       |                    |
|          | 25   |      | L027L 3223L    |       |                    |
|          | 26   |      | 26(M1) 00F     |       |                    |
|          | 27   |      | N227L 41F      |       |                    |
|          |      |      | 00911K         |       | Store Drum Set III |
| 911      | 0    |      | J0335F 50L     |       |                    |
|          | 1    |      | 26(Y1) 002990F |       |                    |
|          | 2    |      | 0040F 263L     |       |                    |
|          | 3    |      | J0400F 503L    |       |                    |
|          | 4    |      | 26(Y1) 003056F |       |                    |
|          | 5    |      | 0030F 26(M1)   |       |                    |
|          |      |      | 26911N         |       |                    |

KSL 1.20